

PROJECTION OPTICAL SYSTEM, PROJECTION TYPE IMAGE DISPLAY
APPARATUS, AND IMAGE DISPLAY SYSTEM

BACKGROUND OF THE INVENTION

1.FIELD OF THE INVENTION

[0001] The present invention relates generally to a projection optical system for use in a projection type image display apparatus such as a projector, and more particularly, to a projection optical system for projecting an image onto a projection surface in a direction which is oblique to the projection surface.

2.DESCRPTION OF RELATED ART

[0002] Conventionally, projectors or projection type image display apparatuses have been proposed in which an image forming element is illuminated with light from a light source and the modulated light which is transmitted through the image forming element or reflected by the image forming element is enlargingly projected onto a screen by a projection lens to display an image.

[0003] Some of projection optical systems for use in such projectors allow projection in a direction which is oblique to the screen in order to reduce the distance between the screen and the projector.

[0004] For example, Japanese Patent Application Laid-Open No. H05(1993)-100312 has proposed a projection optical system which enlargingly projects an image produced on the basis of an original image formed on an image forming

element onto a screen. In the projection optical system, a wide-angle lens with a wide field angle is used, and the image forming element and the screen are disposed with a displacement from the optical axis of the projection optical system to use marginal portions of the field angle for the projection, thereby projecting the image in a direction oblique to the screen.

[0005] Japanese Patent Application Laid-Open No. H05(1993)-080418 has proposed a projection optical system which forms an intermediate image of luminous flux from an image forming element by a first projection optical system and enlargingly projects the intermediate image onto a screen by a second projection optical system. In the projection optical system, the optical axes of the first and second projection optical systems are appropriately inclined to project the image onto the screen in a direction oblique to the screen.

[0006] Domestic re-publication of PCT international publication for patent application W097/01787 (corresponding to U.S Patent No. 5,871,266) has disclosed a projection optical system which realizes oblique projection by using a plurality of reflective surfaces.

[0007] Japanese Patent No. 2786796 has disclosed a projection optical system in which light incident on an ellipsoidal mirror at a first focal point is guided to a second focal point which is disposed to match a focal point of a parabolic mirror, and the light guided to the focal

point of the inclined parabolic mirror is projected as collimated light onto a screen in a direction oblique to the screen.

[0008] Japanese Patent Application Laid-Open No. 2001-264627 has proposed an oblique projection optical system which includes an image forming optical system 602 with a positive optical power and a curved mirror 603 with a negative optical power and provides a positive optical power in total to project an image onto a screen 605, as shown in Fig. 11.

[0009] In the projection optical system proposed in Japanese Patent Application Laid-Open No. H05(1993)-100312, since the image forming element and the screen are displaced from the optical axis, a smaller amount of luminous flux passes through an entrance pupil in a portion of the field angle off the optical axis to cause uneven brightness in the projected image. In addition, the displacement of the image forming element from the optical axis leads to an increase in the size of the projection optical system.

[0010] In the projection optical system proposed in Japanese Patent Application Laid-Open No. H05(1993)-080418, the lens systems are only tilted. Thus, an increased number of lenses are needed to eliminate an astigmatic difference and sufficiently incline an image surface.

[0011] The projection optical system proposed in Domestic re-publication of PCT international publication for patent application WO97/01787 uses one concave mirror and one or

two convex mirrors to form a coaxial optical system and projects an image in an oblique direction by partially using reflective surfaces of the concave mirror and the convex mirror(s). When the coaxial optical system is used, however, it is difficult to correct aberration and provide a brighter reflective optical system, that is, have a smaller F number.

[0012] In the projection optical system disclosed in Japanese Patent No. 2786796, light rays other than the principal ray do not pass through the first focal point of the ellipsoidal mirror to produce aberration, and the same light rays again cause aberration since the rays do not pass through the second focal point of the ellipsoidal mirror. The image of the light is enlarged at the time of the incidence on the parabolic mirror, so that greater aberration is produced on the screen to significantly degrade performance of image formation.

[0013] The projection optical system proposed in Japanese Patent Application Laid-Open No. 2001-264627 does not form an intermediate image since the overall system has the positive optical power. Thus, eliminating distortion of an image without affecting performance of image formation requires the curved mirror with the negative optical power disposed close to the screen, but the curved mirror has a large size.

SUMMARY OF THE INVENTION

[0014] It is an object of the present invention to provide

a projection optical system which can project a bright image with less distortion and has a short projection distance without causing an increase in aperture, producing aberration due to large decentering, and causing an increase in size of a reflective surface, and a projection type image display apparatus having the projection optical system.

[0015] To achieve the object, according to one aspect of the present invention, provided a projection optical system which projects luminous flux from an original image onto a projection surface which is oblique to a central principal ray which is a principal ray of luminous flux traveling from the center of the original image to the center of a projected image. The projection optical system comprises a refractive optical system which includes a plurality of refractive optical elements through which the luminous flux from the original image passes through, and a reflective optical system which includes a plurality of reflective surfaces each having an optical power and guides the luminous flux emerging from the refractive optical system to the projection surface.

[0016] These and other characteristics of the projection optical system and the projection type image display apparatus according to the present invention will be apparent from the following description of specific embodiments with reference to the drawings.

BRIEF DESCRIPTION OF THE DRAWINGS

[0017] Fig. 1(A) is a schematic diagram showing all optical systems of a rear projector which is Embodiment 1 of the present invention, and Fig. 1(B) is an enlarged view schematically showing a projection optical system of all the optical systems;

[0018] Fig. 2(A) shows distortion of the rear projector shown in Fig. 1(A), and Fig. 2(B) is a spot diagram of the rear projector shown in Fig. 1(A);

[0019] Fig. 3(A) is a schematic diagram showing all optical systems of a rear projector which is Embodiment 2 of the present invention, and Fig. 3(B) is an enlarged view schematically showing a projection optical system of all the optical systems;

[0020] Fig. 4(A) shows distortion of the rear projector shown in Fig. 3(A), and Fig. 4(B) is a spot diagram of the rear projector shown in Fig. 3(A);

[0021] Fig. 5 is a schematic diagram particularly showing a projection optical system of all optical systems of a rear projector which is Embodiment 3 of the present invention;

[0022] Fig. 6(A) shows distortion of the rear projector shown in Fig. 5, and Fig. 6(B) is a spot diagram of the rear projector shown in Fig. 5;

[0023] Fig. 7 is a schematic diagram particularly showing a projection optical system of all optical systems of a rear projector which is Embodiment 4 of the present invention;

[0024] Fig. 8(A) shows distortion of the rear projector shown in Fig. 7, and Fig. 8(B) is a spot diagram of the rear

projector shown in Fig. 7;

[0025] Fig. 9 is a schematic diagram particularly showing a projection optical system of all optical systems of a rear projector which is Embodiment 5 of the present invention;

[0026] Fig. 10(A) shows distortion of the rear projector shown in Fig. 9, and Fig. 10(B) is a spot diagram of the rear projector shown in Fig. 9; and

[0027] Fig. 11 is a schematic diagram showing a conventional projection optical system.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

[0028] Prior to description of Embodiments of the present invention, description is made for matters common to all of Embodiments.

[0029] In Embodiments of the present invention, a light ray emerging from the center of an original image displayed on an image forming element to the center of a projected image on a projection surface through the center of a pupil (an aperture stop) is referred to as a central principal ray (or a reference axis ray).

[0030] When the center cannot be defined in azimuthal directions with no symmetry of the image forming element and the pupil (the aperture stop), the barycenter of each of them is defined as the center. However, the present invention is also applicable when a path (a reference axis) of the central principal ray can be considered as the substantial center of each of them in Embodiments of the

present invention.

[0031] In Embodiments of the present invention, section views and numerical data of optical systems are shown. Projection optical systems of Embodiments have aspheric surfaces which are rotationally asymmetric, and the shape of the surface is represented by the following expression:

$$z=C02y^2+C20x^2+C03y^3+C21x^2y+C04y^4+C22x^2y^2+C40x^4 \\ +C05y^5+C23x^2y^3+C41x^4y+C06y^6+C24x^2y^4+C42x^4y^2+C60x^6 \quad (1)$$

[0032] Each of the rotationally asymmetric surfaces in Embodiments has a plane-symmetric shape which has a yz plane as a plane of symmetry since the above expression has only even-numbered order terms for x and no odd-numbered order terms.

[0033] It should be noted that, while Embodiments of the present invention employ the expression with a sixth order for representing the surface, the present invention is applicable without being limited to any particular order for defining the surface shape. The shape of each surface may be represented by another expression such as the Zernike polynomial.

[0034] Next, the concepts in each of Embodiments are described. In a projection type image display apparatus, an image forming element modulates illumination light to form an image (an original image), and a projection optical system enlarges luminous flux emerging from the image forming element and guides the luminous flux to form an image on a projection surface or an image surface.

[0035] The projection is performed obliquely such that the central principal ray of the luminous flux guided to the projection surface is projected at an angle not perpendicular to the projection surface. The oblique projection of the projection optical system onto the projection surface causes less interference of a projection of the projection optical system to the projection surface as compared with perpendicular projection when viewed from a direction of the normal line to the projection surface.

[0036] An angle between the central principal ray and the normal line to the projection surface, that is, an oblique projection angle may be increased to eliminate the interference, and a plane folding mirror may be used to fold the optical path. This can realize a thin rear projector (a rear projection type image display apparatus), for example.

[0037] To enhance performance of image formation, on the projection surface, of light from the original image on the image forming element at a large oblique projection angle, the projection optical system must allow ready correction of an astigmatic difference, curvature of field, distortion, and trapezoidal distortion which occur significantly due to decentering of the image surface.

[0038] When an image on an object surface is proportionally enlarged to an image on the image surface, the relationship between the focal length at the azimuth in the decentering direction and the focal length at the azimuth orthogonal thereto is such that the focal length at

the azimuth orthogonal to the decentering direction is equal to the value determined by multiplying the focal length at the azimuth in the decentering direction by the cosine of the oblique projection angle if the image surface is decentered to realize the projection optical system of the oblique projection type.

[0039] In other words, the focal length depends on the azimuth of the central principal ray. This is described, for example, in Japanese Patent Application Laid-Open No.2001-255462.

[0040] Thus, azimuth dependence of the focal length of the overall optical system must be provided by having azimuth dependence of the optical power of each optical surface within the projection optical system for the oblique projection.

[0041] To realize such a projection optical system, each of Embodiments of the present invention employs a projection optical system formed of a refractive optical system and a reflective optical system.

[0042] For aberration correction to be made by the two optical systems, the refractive optical system mainly corrects spherical aberration and comatic aberration, and reflective surfaces having optical powers of the reflective optical system correct an astigmatic difference, curvature of field, distortion, and trapezoidal distortion which need considerable correction due to the large oblique projection angle.

[0043] The ratio of a focal length f_a of the reflective optical system to a focal length f of the overall projection optical system desirably satisfies the following:

$$|f_a/f| > 2 \quad (2)$$

[0044] As the ratio is smaller, light rays are incident on the reflective optical system at a smaller height. Particularly, when the ratio is equal to or lower than the lower limit in the expression (2), the height of the light rays is extremely small to require stronger azimuth dependence of radius of curvature in order to make correction of azimuth dependence of the focal length necessary for the oblique projection of the central principal ray onto the projection surface. Consequently, other types of aberration are difficult to correct.

[0045] The astigmatic difference and curvature of field are corrected by a rotationally asymmetric surface such as a free-form surface, an anamorphic surface, or a toric surface which allows flexible design of the optical power for each azimuth.

[0046] When each optical surface is tilted or shifted, the effect of correction of aberration which occurs due to the oblique projection is increased. To provide the optical power varying depending on the azimuth, a rotationally symmetric surface may be decentered.

[0047] For optical power distribution between the refractive optical system and the reflective optical system, an excessively great power provided for the refractive

optical system in the projection optical system results in an extremely small height of the light ray incident on a reflective surface of the reflective optical system. It is thus difficult to provide azimuth dependence of the optical power acting on the light ray in the reflective optical system. In other words, correction of the astigmatic difference is difficult.

[0048] On the other hand, if the optical power of the refractive optical system is excessively reduced, luminous flux is incident on the reflective surface at a light ray height which remains large. In this case, the number of reflective surfaces in the reflective optical system must be increased to correct the astigmatic difference, distortion, and trapezoidal distortion. In addition, luminous flux of the off-axis light ray is diverged to cause an increase in the size of the reflective optical system.

[0049] When a plane folding mirror is provided between the reflective optical system and the projection surface, the optical path can be folded before incidence on the inclined projection surface. Thus, the overall optical path can be folded to reduce the thickness. When this is applied, for example, to a rear projector, a thin rear projector can be realized.

[0050] When the projection optical system has an intermediate image forming position at an optical surface close to the image surface, the height of the light ray at optical surfaces closer to the image surface becomes smaller

to facilitate correction of distortion with optical power distribution which has less influence on the astigmatic difference. In addition, the distortion can be corrected even when the angle (the oblique projection angle) between the central principal ray and the projection surface is large.

[0051] When the optical power is asymmetric in the azimuthal direction of 0 and 90 degrees in an optical surface near the intermediate image forming position, a flexible relationship is established between the object height and the focal length, thereby allowing correction of distortion even at a large oblique projection angle.

[0052] An optical surface closer to or closest to the intermediate image forming position can be formed as a reflective surface to correct large distortion with a small number of optical surfaces since the reflective surface can provide a larger optical power than the refractive surface.

[0053] The concave and convex shapes of the intermediate image forming surface caused by the curvature of field are matched with the concave and convex shapes of an optical surfaces near the intermediate image forming surface, so that the distortion can be corrected favorably.

[0054] In the projection optical system, each of optical surfaces having optical powers disposed immediately before and after the intermediate image forming surface may be shaped in the azimuthal directions of 0 and 90 degrees such that the surface has a concave shape toward each azimuthal

direction when the refractive optical system has negative curvature of field and the surface has a convex shape toward each azimuthal direction when the refractive optical system has positive curvature of field. This can realize the projection optical system which can correct the distortion with a small number of optical surfaces even at a large angle formed between the central principal ray and the projection surface.

[0055] Next, specific embodiments of the present invention are described with reference to the drawings. Design data corresponding to Embodiments 1 to 5 are shown below in Tables 1 to 5 as Numerical Examples 1 to 5.

[0056] Table 6 shows values of the expression (2), vertical and horizontal dimensions of image forming elements (for example, reflective type liquid crystal display panels), effective F numbers, vertical and horizontal dimensions of screens (projection surfaces), focal lengths f_a of refractive optical systems, focal lengths f of projection optical systems in longitudinal directions of the screens, and oblique projection angles θ of central principal rays projected onto the screens, in Numerical Examples 1 to 5.

[0057] (Embodiment 1)

Fig. 1(A) shows the structure of all optical systems of a rear projector (a projection type image display apparatus) which is Embodiment 1 of the present invention. While Embodiment 1 employs a reflective type liquid crystal panel (element) as an image forming element, the present

invention is applicable to an apparatus using a transmissive type image forming element. In addition to the liquid crystal element, other image forming elements can be used as the image forming element, such as a self-light-emission element (for example, an organic or inorganic electroluminescence element) and a micromirror device.

[0058] Fig. 1(B) shows a projection optical system 10 which is a main part of all the optical systems.

[0059] In Figs. 1(A) and 1(B), reference numeral 1 shows a reflective type liquid crystal panel (the image forming element) which is connected to a driving circuit 20 as shown in Fig. 1(B). The driving circuit 20 receives image information from an image information supply apparatus 25 such as a personal computer, a VCR, a television, a DVD player, a camera (a video camera, a digital camera or the like), a cellular phone, and a radio wave receiver (wired or wireless). An image display system is formed in this manner. The driving circuit 20 drives the reflective type liquid crystal panel 1 such that an original image corresponding to the input image information is displayed on the reflective type liquid crystal panel 1. This structure is also used in other Embodiments later described, although not shown.

[0060] Upon incidence of illumination light from an illumination system, not shown, the reflective type liquid crystal panel 1 modulates the light into image light and reflects the light. The image light modulated and reflected by the reflective type liquid crystal panel 1 is first

incident on a refractive optical system 2 of the projection optical system 10.

[0061] The refractive optical system 2 is disposed at a position closer to the reflective type liquid crystal panel 1 serving as an object surface in all the optical systems, where the refractive optical system 2 receives the light from the reflective type liquid crystal panel 1 at a large height of light rays, and mainly corrects spherical aberration and comatic aberration. The refractive optical system 2 is formed of lenses which are rotationally symmetric with respect to the central principal ray from the reflective type liquid crystal panel 1. The refractive optical system 2 of Embodiment 1 is formed of five spherical lenses. The number of the spherical lenses, however, is not limited thereto in the refractive optical system of the present invention. A rotationally asymmetric spherical surface may also be used in the refractive optical system to improve correction of the spherical aberration.

[0062] Reference numeral 3 shows a reflective optical system of the projection optical system 10, on which the image light emerging from the refractive optical system 2 is incident. The reflective optical system 3 is disposed closer to a screen 5 serving as an image surface relative to the refractive optical system 2 in all the optical systems and mainly corrects distortion and trapezoidal distortion.

[0063] In Embodiment 1, the reflective optical system 3 is formed of four reflective surfaces (a first to a fourth

reflective surface 31 to 34) or mirrors to sequentially reflect the image light from the refractive optical system 2. However, the number of the reflective surfaces is not limited thereto in the reflective optical system of the present invention.

[0064] The reflective optical system 3 is preferably formed of three or more reflective surfaces since an astigmatic difference can be favorably corrected, satisfactory performance of image formation is achieved, and the distortion and trapezoidal distortion can be favorably corrected, even the central principal ray is projected onto the screen 5 at a large oblique projection angle of 42.5 degrees as in Embodiment 1.

[0065] Fig. 2(B) illustrates performance of image formation on the screen of the projection optical system 10 of Embodiment 1. In Fig. 2(B), the horizontal axis and vertical axis represent object heights in a horizontal direction and a vertical direction. Fig. 2(A) shows distortion of an image on the screen. It can be seen from Fig. 2(A) that the projection optical system 10 of Embodiment 1 can excellently correct the distortion and trapezoidal distortion.

[0066] In the reflective optical system 3 shown in Figs. 1(A) and 1(B), each of the first reflective surface 31 and the second reflective surface 32 is disposed at a relatively high position of light rays and corrects azimuth dependence of a focal length and astigmatism. Especially, rotationally

asymmetric surfaces used as the first reflective surface 31 and the second reflective surface 32 can provide varying optical powers depending on the azimuth to enhance the effect of correction.

[0067] Each of the third reflective surface 33 and the fourth reflective surface 34 is disposed at a position close to an intermediate image forming surface M shown in Fig. 1(B) where they receive light rays at a relatively small height, and corrects the distortion. Especially, the intermediate image forming surface M is provided within the reflective optical system 3 to dispose the reflective surfaces near the intermediate image forming surface M, thereby making it possible to reduce the distortion and trapezoidal distortion without affecting spherical aberration and astigmatism.

[0068] In addition, the shape of the intermediate image forming surface M is matched with the shapes of the optical surfaces near the intermediate image forming surface M, so that distortion can be corrected favorably.

[0069] Reference numeral 4 in Fig. 1(A) shows a plane mirror unit which is formed of three plane mirrors including a first to a third plane mirror 41 to 43 to sequentially reflect the image light from the projection optical system (reflective optical system 3) such that the image light is folded. This can reduce the depth dimension (in a lateral direction in Fig. 1(A)) required to form an optical path throughout the projector.

[0070] While Embodiment 1 is described for the case where the plane mirror unit 4 is formed of the three plane mirrors, the number of the plane mirrors is not limited thereto in the present invention.

[0071] The screen 5 is disposed at the image forming surface of the image light emerging from the projection optical system formed of the refractive optical system 2 and the reflective optical system 3 and reflected by the plane mirror unit 4. Thus, a projected image formed by the image light is displayed on the screen 5.

[0072] While Embodiment 1 has been described for the case where the image light is projected onto the screen 5 through the plane mirror unit 4, the image light emerging from the projection optical system formed of the refractive optical system 2 and the reflective optical system 3 may be projected onto the screen 5 without passing through the plane mirror unit 4 to form a so-called front projector.

[0073] (Embodiment 2)

Fig. 3(A) shows all optical systems of a rear projector which is Embodiment 2 of the present invention. Fig. 3(B) shows the structure of a projection optical system 100 which is a main part of all the optical systems.

[0074] All the optical systems of Embodiment 2 are composed of a reflective type liquid crystal panel 1, the projection optical system 100, and a single plane mirror 104. The projection optical system 100 is formed of a refractive optical system 102 and a reflective optical system 103

similarly to Embodiment 1.

[0075] The refractive optical system 102 is formed of seven rotationally symmetric glass lenses, while the reflective optical system 102 is formed of three reflective surfaces (mirrors) 131 to 133.

[0076] An intermediate image forming surface M is provided between the first reflective surface 131 and the second reflective surface 132.

[0077] Fig. 4(B) illustrates performance of image formation on a screen of the projection optical system of Embodiment 2. In Fig. 4(B), the horizontal axis and vertical axis are the same as those in Fig. 2(B). Fig. 4(A) shows distortion of an image on the screen. It can be seen from Fig. 4(A) that distortion can be corrected favorably by the projection optical system of Embodiment 2.

[0078] (Embodiment 3)

Fig. 5 shows the structure of a projection optical system 200 which is a main part of all optical systems of a rear projector which is Embodiment 3 of the present invention. Reference numeral 1 shows a reflective type liquid crystal panel.

[0079] The projection optical system 200 is formed of a refractive optical system 202 and a reflective optical system 203 similarly to Embodiment 1.

[0080] The refractive optical system 202 is formed of six rotationally symmetric glass lenses, while the reflective optical system 203 is formed of five reflective surfaces

(mirrors) 231 to 235.

[0081] An intermediate image forming surface M is provided closer to the fourth reflective surface 234 between the fourth reflective surface 234 and the fifth reflective surface 235.

[0082] Fig. 6(B) illustrates performance of image formation on a screen of the projection optical system of Embodiment 3. The horizontal axis and the vertical axis in Fig. 6(B) are the same as those in Fig. 2(B). Fig. 6(A) shows distortion of an image on the screen. It can be seen from Fig. 6(A) that distortion can be corrected favorably by the projection optical system of Embodiment 3.

[0083] (Embodiment 4)

Fig. 7 shows the structure of a projection optical system 300 which is a main part of all optical systems of a rear projector which is Embodiment 4 of the present invention. Reference numeral 1 shows a reflective type liquid crystal panel.

[0084] The projection optical system 300 is formed of a refractive optical system 302 and a reflective optical system 303 similarly to Embodiment 1.

[0085] The refractive optical system 302 is formed of five rotationally symmetric glass lenses, while the reflective optical system 303 is formed of four reflective surfaces (mirrors) 331 to 334.

[0086] In Embodiment 4, the focal length of the refractive optical system 302 is relatively small at 57 mm ($f_a=57$ mm),

and luminous flux emerges from the refractive optical system 302 with a small width. This is associated with a small height of light rays.

[0087] Thus, the light is incident on the first reflective surface 331 at a small height of light rays, and varying optical powers depending on the azimuth are not easily provided in the reflective optical system 300.

[0088] In Embodiment 4, an intermediate image forming surface M is formed to extend on both sides of the third reflective surface 333.

[0089] The value determined from the expression (2) as the condition of the focal lengths is 4.7 ($|f_a/f|=4.7$).

[0090] Fig. 8(B) illustrates performance of image formation on a screen of the projection optical system of Embodiment 4. The horizontal axis and the vertical axis in Fig. 8(B) are the same as those in Fig. 2(B). Fig. 8(A) shows distortion of an image on the screen. It can be seen from Fig. 8(A) that distortion can be corrected favorably by the projection optical system of Embodiment 4.

[0091] (Embodiment 5)

Fig. 9 shows the structure of a projection optical system 400 which is a main part of all optical systems of a rear projector which is Embodiment 5 of the present invention. Reference numeral 1 shows a reflective type liquid crystal panel.

[0092] The projection optical system 400 is formed of a refractive optical system 402 and a reflective optical

system 403 similarly to Embodiment 1.

[0093] The refractive optical system 402 is formed of five rotationally symmetric glass lenses, while the reflective optical system 403 is formed of four reflective surfaces (mirrors) 431 to 434.

[0094] In Embodiment 5, the focal length of the refractive optical system 402 is relatively large at 100 mm ($f_a=100$ mm), and luminous flux emerges from the refractive optical system 402 with a large width. This is associated with a large height of light rays.

[0095] Thus, the light is incident on the first reflective surface 431 at a large height of light rays, but off-axis light rays are subjected to less refraction due to the large focal length. This results in less divergence of the overall luminous flux, so that the first reflective surface 431 can be formed with small dimensions. The value determined in the expression (2) as the condition of the focal lengths is 8.0 ($|f_a/f|=8.0$).

[0096] In Embodiment 5, an intermediate image forming surface M is formed to extend on both sides of the third reflective surface 433.

[0097] Fig. 10(B) illustrates performance of image formation on a screen of the projection optical system of Embodiment 5. The horizontal axis and the vertical axis in Fig. 10(B) are the same as those in Fig. 2(B). Fig. 10(A) shows distortion of an image on the screen. It can be seen from Fig. 10(A) that distortion can be corrected favorably

by the projection optical system of Embodiment 5.

[0098] Numerical Examples (design data) of Embodiments 1 to 5 are shown below.

[0099] First, description is made for symbols and the like in Numerical Examples.

[0100] When n (n :) is an integer, it represents a surface number. When n is not an integer but "OBJ," "STO," and "IMG" are written instead, the corresponding surface is an object surface, an aperture stop surface, and an image surface, respectively. OBJ corresponds to the surface number 0, and IMG corresponds to the surface number of the final optical surface. For STO, the integer corresponding to n is omitted, and the surface number thereof is determined by adding one to the number n of the preceding surface.

[0101] RDY represents a radius of curvature of the surface. THI represents a spacing between the surface and the next surface. RMD represents a reflection mode of the surface. Numerical Examples below show data only in the reflection mode in which all light rays incident on the surface are reflected.

[0102] XDE, YDE, and ZDE represent an amount of shifting of the origin of a surface shape from the origin of coordinates of a first surface serving as a reference, and specifically, represent the shifting in a +x direction, a +y direction, and a +z direction, respectively.

[0103] ADE, BDE, and CDE represent an amount of tilt of

the origin of a surface with respect to the origin of coordinates of the first surface serving as a reference, and specifically, represent the tilt in a -x direction, a -y direction, and a +z direction, respectively, in a right-handed direction.

[0104] GLB Gn: the origin and coordinates of a surface are represented by decentering from the origin and coordinates of an Sn surface by the amounts of XDE, YDE, ZDE, ADE, BDE, and CDE.

[0105] DAR: when GLB Gn is not specified for a surface, the position of the origin and coordinates of the next surface to the surface are defined by a coordinate system with no decentering from the surface. The origin and coordinates of the next surface are shifted parallel in the +Z direction by a spacing between surfaces specified by THI of the surface.

[0106] GLA represents a glass name of a surface represented by a surface number. A blank in the field of the glass name means air.

[0107] Description is made for a specific example of a surface shape represented by the following data.

```
14:      85.13274      5.000000      SPHM52_OHARA
      XDE: 0.000000   YDE: -0.174089   ZDE: 86.646241   GLB G1
      ADE: 0.000000   BDE: 0.000000   CDE: 0.000000
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[0108] This data means the origin of a fourteenth surface positioned on coordinates shifted from the origin of the first surface relative to the coordinates of the first

surface by the amounts of 0 in the +x direction, -0.174089 in the +y direction, and 86.646241 in the +z direction, and a right-handed orthogonal coordinate system tilted in a right-handed direction by 0 degrees in the -x direction, the -y direction, and +z direction.

[0109] The radius of curvature is 85.13274. The origin and coordinates of the next surface (a fifteenth surface) are at positions shifted parallel in the +z direction by 5.000000 from the origin and coordinates of the fourteenth surface.

[0110] When data about a surface shape includes "UDS" in the line next to "n:" representing the surface number, the surface shape of the optical surface, the position of the origin and coordinate system, reflection mode, and glass data are represented as follows:

13: -475.44862 0.000000 REFL

UDS:

C02: -1.0421E-03 C03: 1.3534E-08 C04: 4.3240E-08

C05: 4.4071E-11 C06: -4.7363E-12 C20: -4.3768E-04

C21: 3.0782E-06 C22: 7.3085E-08 C23: -2.3781E-11

C24: -1.3592E-11 C40: 2.6601E-08 C41: 4.0347E-10

C42: -5.0835E-12 C60: 1.9177E-12

XDE: 0.000000 YDE: -0.174 ZDE: 220.54 GLB-G1

ADE: -13.421914 BDE: 0.000000 CDE: 0.000000

[0111] Description is made mainly for data which has been not described in the data shown earlier. The surface number is 13 which means a thirteenth surface. When a coefficient Cjk: (j and k are integers equal to or larger than zero) is

written, for example, as follows:

C42: -5.0835E-12

then it means that -5.0835E-12 is substituted into the coefficient C42 in the expression (1). "E-X" represents " $\times 10^{-X}$ ". The function derived by similarly substituting all coefficients Cjk into the expression (1) represents the shape of the surface.

[0112]

(Table 1) Numerical Example 1

	RDY	THI	RMD	GLA	
OBJ:	INFINITY	0.000000			
XDE:	0.000000	YDE:	0.000000	ZDE:	0.000000 DAR
ADE:	-10.000000	BDE:	0.000000	CDE:	0.000000
>1:	INFINITY	0.000000			
2:	INFINITY	0.000000		SBSL7_OHARA	
XDE:	0.000000	YDE:	0.000000	ZDE:	0.507713 GLB
G1					
ADE:	-10.000000	BDE:	0.000000	CDE:	0.000000
3:	INFINITY	0.000000			
XDE:	0.000000	YDE:	0.000000	ZDE:	3.553892 GLB
G1					
ADE:	-10.000000	BDE:	0.000000	CDE:	0.000000
STO:	INFINITY	0.000000			
XDE:	0.000000	YDE:	-0.174089	ZDE:	54.034379 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

5: 150.36240 0.000000 SFSL5_OHARA

XDE: 0.000000 YDE: -0.174089 ZDE: 55.263940 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

6: -50.01189 0.000000

XDE: 0.000000 YDE: -0.174089 ZDE: 59.263940 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

7: -92.24522 0.000000 SLAH60_OHARA

XDE: 0.000000 YDE: -0.174089 ZDE: 62.263940 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

8: 68.21463 0.000000 SNSL36_OHARA

XDE: 0.000000 YDE: -0.174089 ZDE: 64.263940 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

9: -54.40654 0.000000

XDE: 0.000000 YDE: -0.174089 ZDE: 69.263940 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

10: 126.65317 0.000000 SLAH60_OHARA
 XDE: 0.000000 YDE: -0.174089 ZDE: 75.548408 GLB
 G1
 ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

11: 84.51358 0.000000 SFSL5_OHARA
 XDE: 0.000000 YDE: -0.174089 ZDE: 77.548408 GLB
 G1
 ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

12: -98.44155 0.000000
 XDE: 0.000000 YDE: -0.174089 ZDE: 85.548408 GLB
 G1
 ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

13: -475.44862 0.000000 REFL
 UDS:
 C02: -1.0421E-03 C03: 1.3534E-08 C04: 4.3240E-08
 C05: 4.4071E-11 C06: -4.7363E-12 C20: -4.3768E-04
 C21: 3.0782E-06 C22: 7.3085E-08 C23: -2.3781E-11
 C24: -1.3592E-11 C40: 2.6601E-08 C41: 4.0347E-10
 C42: -5.0835E-12 C60: 1.9177E-12
 XDE: 0.000000 YDE: -0.174089 ZDE: 220.548408 GLB
 G1
 ADE: -13.421914 BDE: 0.000000 CDE: 0.000000

14: -576.18087 0.000000 REFL

UDS:

C02: -8.6142E-04 C03: 5.4898E-06 C04: 9.1071E-08

C05: 1.7782E-10 C06: -2.9828E-11 C20: 6.4754E-04

C21: 9.2622E-06 C22: 4.1228E-08 C23: 1.6016E-10

C24: -4.3180E-11 C40: -1.1311E-08 C41: 8.7024E-10

C42: -1.9390E-11 C60: -3.5901E-13

XDE: 0.000000 YDE: 49.497533 ZDE: 122.401936 GLB

G1

ADE: -42.843829 BDE: 0.000000 CDE: 0.000000

15: -9686.82349 0.000000 REFL

UDS:

C02: 1.0000E-05 C03: 6.6212E-06 C04: 1.6623E-07

C05: 2.1998E-09 C06: -3.0741E-19 C20: 1.2500E-03

C21: 1.2952E-05 C22: 8.0875E-08 C23: 4.2216E-09

C24: 3.6013E-11 C40: -1.2003E-07 C41: 3.3227E-09

C42: 2.2746E-11 C60: 5.6065E-12

XDE: 0.000000 YDE: -74.587707 ZDE: 197.420954 GLB

G1

ADE: -26.843829 BDE: 0.000000 CDE: 0.000000

16: 177.53352 0.000000 REFL

UDS:

C02: 2.5656E-03 C03: -9.5763E-06 C04: 6.4378E-08

C05: -2.0214E-11 C06: -1.7730E-12 C20: 4.2351E-03

C21: -1.8406E-05 C22: 1.2069E-07 C23: -2.5036E-10

C24: 6.7620E-13 C40: 1.0527E-09 C41: 1.5749E-10
 C42: -1.8899E-13 C60: 3.3698E-13
 XDE: 0.000000 YDE: -87.618965 ZDE: 53.007706 GLB
 G1
 ADE: -16.186914 BDE: 0.000000 CDE: 0.000000

 17: INFINITY 0.000000
 XDE: 0.000000 YDE: -163.766059 ZDE: 152.137017 GLB
 G1
 ADE: -37.530000 BDE: 0.000000 CDE: 0.000000

 18: INFINITY 840.000000 AIR
 XDE: 0.000000 YDE: -163.766059 ZDE: 152.137017 GLB
 G1
 ADE: -37.530000 BDE: 0.000000 CDE: 0.000000

 IMG: INFINITY 0.000000
 XDE: 0.000000 YDE: 0.000000 ZDE: 0.000000 DAR
 ADE: 42.530000 BDE: 0.000000 CDE: 0.000000

[0113]

(Table 2) Numerical Example 2

	RDY	THI	RMD	GLA		
OBJ:	INFINITY	0.000000				
XDE:	0.000000	YDE:	0.000000	ZDE:	0.000000	DAR
ADE:	12.000000	BDE:	0.000000	CDE:	0.000000	
>1:	INFINITY	0.000000				
2:	INFINITY	0.000000		SBSL7_OHARA		
XDE:	0.000000	YDE:	0.000000	ZDE:	0.511170	GLB G1
ADE:	12.000000	BDE:	0.000000	CDE:	0.000000	
3:	INFINITY	0.000000				
XDE:	0.000000	YDE:	0.000000	ZDE:	3.578192	GLB G1
ADE:	12.000000	BDE:	0.000000	CDE:	0.000000	
STO:	INFINITY	0.000000				
XDE:	0.000000	YDE:	0.209714	ZDE:	51.807426	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
5:	51.55033	0.000000		STIH53_OHARA		
XDE:	0.000000	YDE:	0.209714	ZDE:	51.907426	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
6:	799.18006	0.000000				
XDE:	0.000000	YDE:	0.209714	ZDE:	57.907426	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	

7:	-371.00181	0.000000	STIH14_OHARA	
XDE:	0.000000	YDE:	0.209714	ZDE: 69.369649 GLB G1
ADE:	0.000000	BDE:	0.000000	CDE: 0.000000
8:	35.66047	0.000000		
XDE:	0.000000	YDE:	0.209714	ZDE: 71.369649 GLB G1
ADE:	0.000000	BDE:	0.000000	CDE: 0.000000
9:	35.66047	0.000000	SFSL5_OHARA	
XDE:	0.000000	YDE:	0.209714	ZDE: 71.369649 GLB G1
ADE:	0.000000	BDE:	0.000000	CDE: 0.000000
10:	-49.42587	0.000000		
XDE:	0.000000	YDE:	0.209714	ZDE: 78.893922 GLB G1
ADE:	0.000000	BDE:	0.000000	CDE: 0.000000
11:	INFINITY	0.000000		
XDE:	0.000000	YDE:	0.209714	ZDE: 78.993922 GLB G1
ADE:	0.000000	BDE:	0.000000	CDE: 0.000000
12:	333.80929	0.000000	SFSL5_OHARA	
XDE:	0.000000	YDE:	0.209714	ZDE: 80.993922 GLB G1
ADE:	0.000000	BDE:	0.000000	CDE: 0.000000
13:	-26.69819	0.000000	AIR	
XDE:	0.000000	YDE:	0.209714	ZDE: 88.993922 GLB G1

ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
14:	-26.69819		0.000000		STIH14_OHARA	
XDE:	0.000000	YDE:	0.209714	ZDE:	88.993922	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
15:	-75.89572		0.000000			
XDE:	0.000000	YDE:	0.209714	ZDE:	90.993922	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
16:	-144.20675		0.000000		STIM22_OHARA	
XDE:	0.000000	YDE:	0.209714	ZDE:	110.832117	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
17:	220.20414		0.000000			
XDE:	0.000000	YDE:	0.209714	ZDE:	112.732117	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
18:	220.20414		0.000000		STIH53_OHARA	
XDE:	0.000000	YDE:	0.209714	ZDE:	112.732117	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
19:	-86.83039		0.000000			
XDE:	0.000000	YDE:	0.209714	ZDE:	119.095822	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
20:	333.01970		0.000000		REFL	

UDS:

C02: 1.5692E-03 C03: -2.5402E-05 C04: 3.9380E-07
C05: -1.4236E-09 C06: -5.9631E-12 C20: 1.1891E-03
C21: -1.8773E-05 C22: 7.8122E-07 C23: -9.6285E-09
C24: 3.8581E-11 C40: 1.2704E-07 C41: -3.9562E-09
C42: 1.7082E-11 C60: 1.9672E-11
XDE: 0.000000 YDE: -24.790286 ZDE: 254.938227 GLB

G1

ADE: -12.000000 BDE: 0.000000 CDE: 0.000000

21: 154.77744 0.000000 REFL

UDS:

C02: 3.1081E-03 C03: 1.2200E-05 C04: 4.8036E-08
C05: 9.3762E-10 C06: 3.1956E-12 C20: 4.5729E-03
C21: 1.9204E-05 C22: 1.2304E-07 C23: 1.4581E-09
C24: 2.0784E-12 C40: 2.9355E-08 C41: 4.4342E-10
C42: -1.3385E-12 C60: -8.7721E-13
XDE: 0.000000 YDE: 70.694664 ZDE: 126.566939 GLB

G1

ADE: -6.000000 BDE: 0.000000 CDE: 0.000000

22: -756.77260 0.000000 REFL

UDS:

C02: -4.7524E-04 C03: -5.5600E-08 C04: 1.5167E-08
C05: -2.3281E-10 C06: 1.2343E-12 C20: -1.1111E-04
C21: -3.1594E-06 C22: 2.7694E-08 C23: -2.1455E-11
C24: -1.6486E-12 C40: -3.2276E-09 C41: 1.1808E-10

C42: -1.3083E-12 C60: -1.9889E-13
 XDE: 0.000000 YDE: 98.244332 ZDE: 274.062165 GLB
 G1
 ADE: -32.595876 BDE: 0.000000 CDE: 0.000000

23: INFINITY 0.000000 REFL
 XDE: 0.000000 YDE: 439.535441 ZDE: 196.471061 GLB G1
 ADE: -25.191752 BDE: 0.000000 CDE: 0.000000

24: INFINITY 0.000000
 XDE: 0.000000 YDE: 637.325349 ZDE: 587.888510 GLB G1
 ADE: -25.191752 BDE: 0.000000 CDE: 0.000000

25: INFINITY 0.000000
 XDE: 0.000000 YDE: 637.325349 ZDE: 587.888510 GLB G1
 ADE: -25.191752 BDE: 0.000000 CDE: 0.000000

26: INFINITY 0.000000
 XDE: 0.000000 YDE: 637.325349 ZDE: 587.888510 GLB G1
 ADE: -25.191752 BDE: 0.000000 CDE: 0.000000

IMG: INFINITY 0.000000
 XDE: 0.000000 YDE: 0.000000 ZDE: 0.000000 DAR
 ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

[0114]

(Table 3) Numerical Example 3

	RDY	THI	RMD	GLA
OBJ:	INFINITY	0.000000		
XDE:	0.000000	YDE:	0.000000	ZDE: 0.000000 DAR
ADE:	-10.000000	BDE:	0.000000	CDE: 0.000000
>1:	INFINITY	0.000000		
2:	INFINITY	0.000000		SBSL7_OHARA
XDE:	0.000000	YDE:	0.000000	ZDE: 0.507713 GLB G1
ADE:	-10.000000	BDE:	0.000000	CDE: 0.000000
3:	INFINITY	0.000000		
XDE:	0.000000	YDE:	0.000000	ZDE: 3.553892 GLB G1
ADE:	-10.000000	BDE:	0.000000	CDE: 0.000000
STO:	INFINITY	0.000000		
XDE:	0.000000	YDE:	-0.174089	ZDE: 54.000762 GLB G1
ADE:	0.000000	BDE:	0.000000	CDE: 0.000000
5:	-112.90012	0.000000		SFPL51_OHARA
XDE:	0.000000	YDE:	-0.174089	ZDE: 63.332130 GLB G1
ADE:	0.000000	BDE:	0.000000	CDE: 0.000000
6:	-87.95475	0.000000		
XDE:	0.000000	YDE:	-0.174089	ZDE: 66.784623 GLB G1
ADE:	0.000000	BDE:	0.000000	CDE: 0.000000

7:	-113.44236	0.000000	SLAH63_OHARA	
XDE:	0.000000	YDE: -0.174089	ZDE: 67.372727	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
8:	481.88529	0.000000	SPHM52_OHARA	
XDE:	0.000000	YDE: -0.174089	ZDE: 70.906774	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
9:	-56.81882	0.000000		
XDE:	0.000000	YDE: -0.174089	ZDE: 76.590255	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
10:	-29111.03765	0.000000	SFPL51_OHARA	
XDE:	0.000000	YDE: -0.174089	ZDE: 78.095618	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
11:	-79.33847	0.000000		
XDE:	0.000000	YDE: -0.174089	ZDE: 85.429518	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
12:	-2973.93001	0.000000	SNBH8_OHARA	
XDE:	0.000000	YDE: -0.174089	ZDE: 86.394195	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
13:	85.13274	0.000000	SPHM52_OHARA	
XDE:	0.000000	YDE: -0.174089	ZDE: 86.646241	GLB G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

 14: -137.12810 0.000000
 XDE: 0.000000 YDE: -0.174089 ZDE: 94.625320 GLB G1
 ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

 15: -5263.27597 0.000000 REFL
 UDS:
 C02: -8.0153E-05 C03: -2.1390E-06 C04: -4.6612E-08
 C05: 2.9412E-10 C06: 1.1624E-11 C20: -4.8611E-04
 C21: -3.8497E-06 C22: -1.9078E-08 C23: 3.3357E-10
 C24: 2.9493E-11 C40: -4.6113E-09 C41: 3.4122E-11
 C42: -1.4088E-11 C60: -4.0244E-12
 XDE: 0.000000 YDE: -0.174089 ZDE: 164.640376 GLB
 G1
 ADE: 19.996853 BDE: 0.000000 CDE: 0.000000

 16: -1024.07725 0.000000 REFL
 UDS:
 C02: -4.3074E-04 C03: -9.9627E-06 C04: -1.7549E-07
 C05: -8.5322E-10 C06: -1.4868E-11 C20: -1.0726E-03
 C21: -2.1039E-05 C22: -1.8772E-07 C23: -2.5374E-09
 C24: 1.9444E-12 C40: -2.4834E-08 C41: -2.2646E-09
 C42: -3.0846E-11 C60: -1.6474E-11
 XDE: 0.000000 YDE: -67.663406 ZDE: 84.191796 GLB
 G1
 ADE: 14.993565 BDE: 0.000000 CDE: 0.000000

17: -430.10066 0.000000 REFL

UDS:

C02: -1.1063E-03 C03: -7.6973E-06 C04: -5.3566E-08

C05: 7.8632E-10 C06: -2.7924E-12 C20: -6.5187E-04

C21: -1.5238E-05 C22: 3.3919E-08 C23: -1.2372E-10

C24: -2.4055E-12 C40: 3.3204E-08 C41: -1.1056E-09

C42: 1.1430E-11 C60: -1.8272E-12

XDE: 0.000000 YDE: -87.645086 ZDE: 197.437511 GLB

G1

ADE: 9.992618 BDE: 0.000000 CDE: 0.000000

18: -284.47384 0.000000 REFL

UDS:

C02: -1.6663E-03 C03: -1.8203E-05 C04: -7.4191E-07

C05: -5.9931E-09 C06: -9.9019E-11 C20: -4.9757E-05

C21: -7.9485E-06 C22: -1.5758E-07 C23: -9.4057E-09

C24: -1.8063E-10 C40: 7.6347E-08 C41: -1.8720E-09

C42: -3.5187E-11 C60: -2.7941E-12

XDE: 0.000000 YDE: -156.259051 ZDE: 78.555415 GLB

G1

ADE: 7.495871 BDE: 0.000000 CDE: 0.000000

19: -152.65281 0.000000 REFL

UDS:

C02: -3.0700E-03 C03: 1.0401E-05 C04: -5.3480E-08

C05: -3.8871E-10 C06: 5.9757E-12 C20: -3.8750E-03

C21: 1.5556E-05 C22: -4.3126E-08 C23: -7.1974E-10
 C24: 4.4399E-12 C40: 3.8167E-08 C41: -5.3764E-10
 C42: 8.8297E-14 C60: 2.0046E-12
 XDE: 0.000000 YDE: -192.495471 ZDE: 213.790899 GLB
 G1
 ADE: 4.929598 BDE: 0.000000 CDE: 0.000000

 20: INFINITY 0.000000
 XDE: 0.000000 YDE: -255.554100 ZDE: 77.689432 GLB G1
 ADE: 24.859267 BDE: 0.000000 CDE: 0.000000

 21: INFINITY -770.000000
 XDE: 0.000000 YDE: -255.554100 ZDE: 77.689432 GLB
 G1
 ADE: 24.859267 BDE: 0.000000 CDE: 0.000000

 IMG: INFINITY 0.000000
 XDE: 0.000000 YDE: 0.000000 ZDE: 0.000000 DAR
 ADE: -42.530000 BDE: 0.000000 CDE: 0.000000

[0115]

(Table 4) Numerical Example 4

	RDY	THI	RMD	GLA		
OBJ:	INFINITY	0.000000				
XDE:	0.000000	YDE:	0.000000	ZDE:	0.000000	DAR
ADE:	-10.000000	BDE:	0.000000	CDE:	0.000000	
>1:	INFINITY	0.000000				
2:	INFINITY	0.000000		SBSL7_OHARA		
XDE:	0.000000	YDE:	0.000000	ZDE:	0.507713	GLB G1
ADE:	-10.000000	BDE:	0.000000	CDE:	0.000000	
3:	INFINITY	0.000000				
XDE:	0.000000	YDE:	0.000000	ZDE:	3.553892	GLB G1
ADE:	-10.000000	BDE:	0.000000	CDE:	0.000000	
STO:	INFINITY	0.000000				
XDE:	0.000000	YDE:	-0.174089	ZDE:	54.039651	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
5:	135.56340	0.000000		SFSL5_OHARA		
XDE:	0.000000	YDE:	-0.174089	ZDE:	54.139651	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	
6:	-45.08961	0.000000				
XDE:	0.000000	YDE:	-0.174089	ZDE:	57.745962	GLB G1
ADE:	0.000000	BDE:	0.000000	CDE:	0.000000	

7:	-83.16624	0.000000	SLAH60_OHARA	
XDE:	0.000000	YDE: -0.174089	ZDE: 57.845962	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
8:	61.50079	0.000000	SNSL36_OHARA	
XDE:	0.000000	YDE: -0.174089	ZDE: 59.649118	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
9:	-49.05173	0.000000		
XDE:	0.000000	YDE: -0.174089	ZDE: 64.157006	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
10:	114.18768	0.000000	SLAH60_OHARA	
XDE:	0.000000	YDE: -0.174089	ZDE: 64.257006	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
11:	76.19556	0.000000	SFSL5_OHARA	
XDE:	0.000000	YDE: -0.174089	ZDE: 66.060162	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
12:	-88.75271	0.000000		
XDE:	0.000000	YDE: -0.174089	ZDE: 73.272784	GLB G1
ADE:	0.000000	BDE: 0.000000	CDE: 0.000000	
13:	-317.87761	0.000000	REFL	
UDS:				

C02: -1.5262E-03 C03: 2.0955E-07 C04: 1.1412E-07
 C05: 4.8311E-10 C06: -2.6871E-11 C20: -5.4267E-04
 C21: 6.5636E-06 C22: 1.6295E-07 C23: 4.7866E-12
 C24: -6.8866E-11 C40: 5.2940E-09 C41: 9.9791E-10
 C42: -5.5120E-11 C60: 3.5406E-11
 XDE: 0.000000 YDE: -0.174089 ZDE: 143.272784 GLB

G1

ADE: -14.000000 BDE: 0.000000 CDE: 0.000000

14: -327.96980 0.000000 REFL

UDS:

C02: -1.4792E-03 C03: 1.6505E-05 C04: 2.7765E-07
 C05: 1.3709E-09 C06: -8.6752E-11 C20: 1.1806E-03
 C21: 2.0605E-05 C22: 1.2929E-07 C23: 3.1810E-10
 C24: -1.2281E-10 C40: -9.2830E-08 C41: 2.2426E-09
 C42: -1.1577E-10 C60: 2.1012E-11
 XDE: 0.000000 YDE: 33.641813 ZDE: 79.674323 GLB

G1

ADE: -42.000000 BDE: 0.000000 CDE: 0.000000

15: -637.61320 0.000000 REFL

UDS:

C02: -6.7912E-04 C03: 7.0132E-06 C04: 3.5251E-07
 C05: 4.4735E-09 C06: 7.5962E-11 C20: 3.3408E-03
 C21: 9.0411E-06 C22: 8.9026E-07 C23: 7.1560E-09
 C24: -2.2344E-10 C40: -1.0800E-06 C41: 2.1792E-08
 C42: -9.3267E-11 C60: 4.6090E-10

XDE: 0.000000 YDE: -40.971569 ZDE: 130.001685 GLB
G1

ADE: -26.000000 BDE: 0.000000 CDE: 0.000000

16: 123.99598 0.000000 REFL

UDS:

C02: 3.7388E-03 C03: -1.9756E-05 C04: 1.2775E-07

C05: 1.4345E-09 C06: -1.7657E-11 C20: 6.0434E-03

C21: -2.8436E-05 C22: 2.0843E-07 C23: 2.2286E-09

C24: -3.0532E-11 C40: 5.3818E-08 C41: 6.2345E-10

C42: 1.6031E-12 C60: 1.1799E-12

XDE: 0.000000 YDE: -46.468081 ZDE: 51.397899 GLB

G1

ADE: -18.000000 BDE: 0.000000 CDE: 0.000000

17: INFINITY 0.000000

XDE: 0.000000 YDE: -126.816532 ZDE: 147.153454 GLB

G1

ADE: -40.000000 BDE: 0.000000 CDE: 0.000000

18: INFINITY 860.000000 AIR

XDE: 0.000000 YDE: -126.816532 ZDE: 147.153454 GLB

G1

ADE: -40.000000 BDE: 0.000000 CDE: 0.000000

IMG: INFINITY 0.000000

XDE: 0.000000 YDE: 0.000000 ZDE: 0.000000 DAR

ADE: 42.530000 BDE: 0.000000 CDE: 0.000000

[0116]

(Table 5) Numerical Example 5

	RDY	THI	RMD	GLA
OBJ:	INFINITY	0.000000		
XDE:	0.000000	YDE: 0.000000	ZDE: 0.000000	DAR
ADE:	-10.000000	BDE: 0.000000	CDE: 0.000000	
>1:	INFINITY	0.000000		
2:	INFINITY	0.000000		SBSL7_OHARA
XDE:	0.000000	YDE: 0.000000	ZDE: 0.507713	GLB
G1				
ADE:	-10.000000	BDE: 0.000000	CDE: 0.000000	
3:	INFINITY	0.000000		
XDE:	0.000000	YDE: 0.000000	ZDE: 3.553892	GLB
G1				
ADE:	-10.000000	BDE: 0.000000	CDE: 0.000000	
STO:	INFINITY	0.000000		
XDE:	0.000000	YDE: -0.174089	ZDE: 54.044623	GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

5: -97.52818 0.000000 SFSL5_OHARA

XDE: 0.000000 YDE: -0.174089 ZDE: 60.942600 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

6: -38.98560 0.000000

XDE: 0.000000 YDE: -0.174089 ZDE: 67.206129 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

7: -98.94172 0.000000 SLAH60_OHARA

XDE: 0.000000 YDE: -0.174089 ZDE: 71.861677 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

8: 143.10183 0.000000 SNSL36_OHARA

XDE: 0.000000 YDE: -0.174089 ZDE: 74.993442 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

9: -57.77868 0.000000

XDE: 0.000000 YDE: -0.174089 ZDE: 82.822853 GLB

G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

10: -971.83795 0.000000 SLAH60_OHARA
XDE: 0.000000 YDE: -0.174089 ZDE: 85.216122 GLB
G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

11: 383.39484 0.000000 SFSL5_OHARA
XDE: 0.000000 YDE: -0.174089 ZDE: 88.347887 GLB
G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

12: -81.62440 0.000000
XDE: 0.000000 YDE: -0.174089 ZDE: 100.874946 GLB
G1

ADE: 0.000000 BDE: 0.000000 CDE: 0.000000

13: -475.44862 0.000000 REFL

UDS:

C02: -1.3316E-03 C03: -2.7007E-07 C04: -2.0036E-08

C05: 1.5458E-11 C06: -1.1055E-12 C20: -4.4476E-04

C21: 2.4247E-06 C22: -5.1273E-08 C23: 8.4072E-11

C24: -6.7504E-14 C40: -3.3535E-08 C41: 1.4044E-10

C42: 2.4683E-12 C60: 1.3283E-12

XDE: 0.000000 YDE: -0.174089 ZDE: 230.874946 GLB

G1

ADE: -14.000000 BDE: 0.000000 CDE: 0.000000

14: -576.18087 0.000000 REFL

UDS:

C02: -1.0977E-03 C03: 2.2750E-06 C04: -6.5301E-08

C05: 4.4654E-10 C06: -1.4974E-11 C20: 1.1086E-03

C21: 5.5054E-06 C22: -5.9548E-08 C23: 7.0003E-10

C24: -5.3210E-12 C40: -1.4722E-08 C41: 3.1417E-10

C42: -2.3206E-12 C60: -8.5527E-14

XDE: 0.000000 YDE: 70.246646 ZDE: 98.432807 GLB

G1

ADE: -41.000000 BDE: 0.000000 CDE: 0.000000

15: -9686.82349 0.000000 REFL

UDS:

C02: -3.0055E-04 C03: -6.2199E-06 C04: 4.4766E-07

C05: 6.8835E-10 C06: -2.6294E-10 C20: 2.8679E-03

C21: 1.2992E-05 C22: -3.0173E-08 C23: 4.0531E-10

C24: -3.7477E-11 C40: -3.1398E-07 C41: 6.7236E-09

C42: 4.3100E-11 C60: 4.4210E-11

XDE: 0.000000 YDE: -83.466583 ZDE: 210.112005 GLB

G1

ADE: -29.500000 BDE: 0.000000 CDE: 0.000000

16: 177.53352 0.000000 REFL

UDS:

C02: 3.1073E-03 C03: -1.5160E-05 C04: 4.5552E-08

C05: 3.9294E-10 C06: -1.3334E-12 C20: 6.3588E-03

C21: -3.5171E-05 C22: 1.9320E-07 C23: 9.6978E-10

C24: -1.8033E-11 C40: -2.0220E-08 C41: 1.6275E-09
 C42: -1.6513E-11 C60: 4.3042E-12
 XDE: 0.000000 YDE: -75.186788 ZDE: 115.473509 GLB
 G1
 ADE: -25.048835 BDE: 0.000000 CDE: 0.000000

 17: INFINITY 0.000000
 XDE: 0.000000 YDE: -163.725679 ZDE: 203.711056 GLB
 G1
 ADE: -45.097670 BDE: 0.000000 CDE: 0.000000

 18: INFINITY 860.000000 AIR
 XDE: 0.000000 YDE: -163.725679 ZDE: 203.711056 GLB
 G1
 ADE: -45.097670 BDE: 0.000000 CDE: 0.000000

 IMG: INFINITY 0.000000
 XDE: 0.000000 YDE: 0.000000 ZDE: 0.000000 DAR
 ADE: 42.530000 BDE: 0.000000 CDE: 0.000000

[0117]

(Table 6)

		Example 1	Example 2	Example 3	Example 4	Example 5
Expression(2)	$ f_a/f $	5.58	4.68	6.29	4.74	7.99
	panel vertical dimension	18	19	18	18	18
	panel horizontal dimension	10	14	10	10	10
	effective F number	3	2.4	3	3	3
	f_a	65.61	59.52	70.2	57.05	98.85
	f	-11.74	-12.69	-11.15	-12.02	-12.35
	screen vertical dimension	1356	1314	1362	1350	1358
	screen horizontal dimension	754	966	754	758	758
	oblique incident angle θ	42.6	50.9	42.6	42.6	42.6

[0118] In Embodiments 1 to 5, the plane including the central principal ray reflected by the plurality of reflective surfaces (having optical powers) is perpendicular to the screen (the projection surface). However, this is not essential in the present invention. Specifically, the plane including the central principal ray may be substantially parallel to the screen. Alternatively, the normal line to the image display surface of the image forming element (an image display device such as a reflective type liquid crystal panel, a transmissive type liquid crystal panel, a DMD, and a self-light-emission element) may be perpendicular to the normal line to the screen.

[0119] In such a case, a reflective member such as a plane mirror with no optical power can be used between the screen and the final reflective surface (the surface closest to the screen having an optical power) among the plurality of reflective surfaces to direct the optical path of the central principal ray toward the screen. This enables the optical path to be folded while the characteristics of the present invention are maintained, thereby achieving a further reduction in size and thickness of the whole apparatus. Preferably, two or three plane mirrors may be used.

[0120] In each of Embodiments 1 to 5, the optical axis of the refractive optical system may be substantially parallel to the screen or may be substantially perpendicular to the

normal line to the screen. In this event, the normal line to the plane including the reference axis within the reflective optical system may be substantially perpendicular to the normal line to the screen. Alternatively, the normal line to the plane including the reference axis within the reflective optical system may be substantially parallel to the normal line to the screen.

[0121] As described above, according to each of Embodiments 1 to 5, it is possible to realize the projection optical system and the projection type image display apparatus, in which the reflective optical system receives the luminous flux with a large width emerging from the original image and passing through the refractive optical system, and excellent performance of image formation can be provided even with a small F number. In addition, it is possible to realize the projection optical system and the projection type image display apparatus, in which the reflective optical system is formed of the plurality of reflective surfaces to favorably correct the astigmatic difference, curvature of field, distortion, and trapezoidal distortion which require considerable correction due to the oblique projection at a large angle with respect to the projection surface, and the projection distance is short.

[0122] Particularly, when the intermediate image forming surface is formed in the projection optical system, the distortion due to the oblique projection can be corrected near the image forming surface. This also can reduce the

size of the reflective surface.

[0123] When the intermediate image forming surface is formed within the reflective optical system, luminous flux for each field angle can be narrowed at the intermediate image forming surface, so that the size of the reflective surfaces can be reduced. In addition, the distortion and trapezoidal distortion can be corrected favorably with less influence on the spherical aberration and comatic aberration.

[0124] The projection optical system may have at least one reflective surface among the optical surfaces having optical powers disposed immediately before or after the intermediate image forming surface. This arrangement enables correction of the distortion and trapezoidal distortion with a small number of the optical surfaces.

[0125] The projection optical system may have a reflective surface as the optical surface having an optical power closest to the intermediate image forming surface to allow correction of the distortion and trapezoidal distortion without affecting the spherical aberration and comatic aberration.

[0126] It is possible to reduce the astigmatic difference occurring on the image surface due to the oblique projection at a large angle if the following expression is satisfied:

$$|f_a/f| > 2$$

where f_a represents the focal length of the refractive optical system and f represents the focal length of the projection optical system in the longitudinal direction of

the projection surface.

[0127] The reflective surfaces formed of rotationally asymmetric surfaces can provide varying image magnifications depending on the azimuthal direction. Consequently, the distortion and trapezoidal distortion due to the oblique projection can be reduced.

[0128] In the projection optical system, at least one of the optical surfaces having optical powers disposed immediately before and after the intermediate image forming surface may have an asymmetric optical power in the azimuthal directions of 0 and 90 degrees, thereby making it possible to set different focal lengths depending on the azimuthal direction on the projection surface. It is thus possible to realize the projection optical system which can correct the distortion even at a large angle between the central principal ray and the projection surface.

[0129] In the projection optical system, each of the optical surfaces having optical powers disposed immediately before and after the intermediate image forming surface may be shaped in the azimuthal directions of 0 and 90 degrees such that the surface has a concave shape toward each azimuthal direction when the refractive optical system has negative curvature of field and the surface has a convex shape toward each azimuthal direction when the refractive optical system has positive curvature of field. This can realize the projection optical system which can correct the distortion with a small number of optical surfaces even at a

large angle formed between the central principal ray and the projection surface.

[0130] The flat reflective surface provided on the optical path from the reflective optical system to the projection surface may fold and project luminous flux emerging from the reflective optical system onto the projection surface inclined with respect to the central principal ray. Thus, a large image can be provided even with a small depth of the apparatus.

[0131] While preferred embodiments have been described, it is to be understood that modification and variation of the present invention may be made without departing from the scope of the following claims.